

Q.11)	$f(x) = (x - 3)$. Find the Domain and Range.
Sol.11)	$f(x) = (x - 3)$ Domain: $f(x)$ is real for all values of x such that; $x \in R$ \therefore Domain = R Range: let $y = f(x)$ $\Rightarrow y = (x - 3)$ $\Rightarrow y = \begin{cases} (x - 3): x - 3 \geq 0; x \geq 3 \\ -(x + 3): x - 3 < 0; x < 3 \end{cases}$ $y = x - 3; x \geq 3$ $\Rightarrow x = y + 3$ We have, $x \geq 3$ $y + 3 \geq 3$ $y \geq 0$ $y \in [0, \infty)$ $y = -(x - 3); x < 3$ $\Rightarrow y = -x + 3$ $\Rightarrow x = 3 - y$ We have, $x < 3$ $3 - y < 3$ $-y < 0$ $\Rightarrow y > 0 \therefore y \in (0, \infty)$ $y \in [0, \infty)$ and $y \in (0, \infty)$ \therefore Range = $[0, \infty)$ ans. {since, when $x = 3$ then $y = 0$ }
Q.12)	Find Domain and Range of $f(x) = 1 - (x - 2)$
Sol.12)	We have, $f(x) = 1 - (x - 2)$ Domain: $f(x)$ is real for all values of x such that; $x \in R$ \therefore Domain = R Range: let $y = f(x)$ $\Rightarrow y = 1 - (x - 2)$ $\Rightarrow y = \begin{cases} 1 - (x - 2): x - 2 \geq 0; x \geq 2 \\ 1 + (x - 2): x - 2 < 0; x < 2 \end{cases}$ $\Rightarrow y = \begin{cases} -x + 3: x \geq 2 \\ x - 1: x < 2 \end{cases}$ $y = -x + 3; x \geq 2$ $\Rightarrow x = 3 - y$ We have, $x \geq 2$ $3 - y \geq 2$ $-y \geq -1$ $y \leq 1$ $y \in (-\infty, 1]$ $y = x - 1; x < 2$ $\Rightarrow x = y + 1$ We have, $x < 2$ $y + 1 < 2$ $y < 1$ $\Rightarrow y \in (-\infty, 1)$ \therefore Range = $(-\infty, 1]$ ans. {when $x = 2$ then $y = 1 \therefore y = 1$ is included in Range}
Q.13)	Find the Domain & Range of $f(x) = \frac{1}{2 - \sin(3x)}$
Sol.13)	$f(x) = \frac{1}{2 - \sin(3x)}$ Domain: we have, $-1 \leq \sin(3x) \leq 1$ $\Rightarrow 2 - \sin(3x) \neq 0$ \therefore Domain $\neq 0$ $\therefore f(x)$ is real for all values of x such that; $x \in R$ \therefore Domain = R Range: We have, $-1 \leq \sin(3x) \leq 1$ $\Rightarrow 1 \geq -\sin(3x) \geq -1$ (multiply by (-1)) $\Rightarrow -1 \leq -\sin(3x) \leq 1$ $\Rightarrow 1 \leq 2 - \sin(3x) \leq 3$ {adding 2} $\Rightarrow \frac{1}{3} \leq \frac{1}{2 - \sin(3x)} \leq 1$ {if $a < x < b$ then $\frac{1}{b} < \frac{1}{x} < \frac{1}{a}$ }



	$\Rightarrow \frac{1}{3} \leq -f(x) \leq 1$ $\therefore \text{Range} = \left[\frac{1}{3}, 1 \right] \text{ ans.}$	
Q.14)	Find the Domain of $f(x) = \sqrt{\frac{1-(x)}{2-(x)}}$	
Sol.14)	$f(x) = \sqrt{\frac{1-(x)}{2-(x)}}$ <p>Domain: $f(x)$ is real for all values of x such that; $x \in R$</p> $\frac{1-(x)}{2-(x)} \geq 0 \text{ and } 2-(x) \neq 0$ $\Rightarrow \frac{-(1x1-1)}{-(1x1-2)} \geq 0 \text{ and } 1x1 \neq 2 \text{ and } x \neq \pm 2$ $\Rightarrow \frac{(1x1-1)(1x1-2)}{(1x1-2)^2} \geq 0 \dots \{ \text{multiply \& divide by } (x) - 2 \}$ $\Rightarrow (1x1-1)(1x1-2) \geq 0$ <p>FIG-7</p> $1x1 \leq 1 \text{ and } 1x1 > 2$ $\pm x \leq 1 \text{ and } \pm x > 2$ $\Rightarrow x \leq 1 \text{ and } -x \leq 1 \qquad x > 2 \text{ and } -x > 2$ $\Rightarrow x \leq 1 \text{ and } x \geq -1 \qquad x > 2 \text{ and } x < -2$ <p>FIG.8</p> <p>Clearly, common solution is</p> $x \in (-\infty, -2) \cup [-1, 1] \cup (2, \infty) \text{ ans.}$	
Q.15)	If $f(x) = \frac{x+1}{x-1}$, find $f(f(x))$.	
Sol.15)	<p>We have, $f(x) = \frac{x+1}{x-1}$</p> <p>Now, $f(f(x)) = f\left(\frac{x+1}{x-1}\right)$</p> $= \frac{\frac{x+1}{x-1} + 1}{\frac{x+1}{x-1} - 1}$ $= \frac{\frac{x+1+x-1}{x-1}}{\frac{x+1-x+1}{x-1}}$ $= \frac{2x}{2}$ $= x \text{ ans.}$	
Q.16)	Let $f = \{(1,1), (2,3), (0,-1), (-1,-3)\}$ be a linear function. Find $f(x)$.	
Sol.16)	<p>Let $f(x) = ax + b$</p> <p>$(1,1) \in f \Rightarrow x = 1 \text{ and } f(x) = 1$</p> $\therefore 1 = a + b \dots\dots\dots (1)$ <p>$(2,3) \in f \Rightarrow x = 2 \text{ and } f(x) = 3$</p> $\therefore 3 = 2a + b \dots\dots\dots (2)$ <p>Solving (1) and (2)</p> $b = -1 \text{ and } a = 2$ $\therefore f(x) = 2x - 1 \text{ ans.}$	
Q.17)	$f(x) = \begin{cases} x^2: 0 \leq x \leq 3 \\ 3x: 3 \leq x \leq 10 \end{cases}$ <p>and $g(x) = \begin{cases} x^2: 0 \leq x \leq 2 \\ 3x: 2 \leq x \leq 10 \end{cases}$, Show that f is a function but g is not a function .</p>	
Sol.17)	<p>We have, $f(x) = \begin{cases} x^2: 0 \leq x \leq 3 \\ 3x: 3 \leq x \leq 10 \end{cases}$</p> $\therefore f = \{(0,0), (1,1), (2,4), (3,9), (4,12), (5,15), (6,18), (7,21), (8,24), (9,27), (10,30)\}$ <p>Clearly, first element of each ordered pair is different (or) each element has unique image $\therefore f$ is</p>	



	<p>a function</p> <p>Now, $g(x) = \begin{cases} x^2: 0 \leq x \leq 2 \\ 3x: 2 \leq x \leq 10 \end{cases}$</p> <p>$\therefore g = \{(0,0), (1,1), (2,4), (3,9), (4,12), (5,15), (6,18), (7,21), (8,24), (9,27), (10,30)\}$</p> <p>Clearly element 2 has two different images 4 and 6</p> <p>$\therefore g$ is not a function</p>	
Q.18)	Let $A = \{9,10,11,12,13\}$; let $f: A \rightarrow N$ be defined by $f(n) =$ highest prime factor of n . Find the range of f .	
Sol.18)	<p>$A = \{9,10,11,12,13\}$</p> <p>$f(n) =$ highest prime factor of n</p> <p>$f(9) =$ highest prime factor of $9 = 3$</p> <p>$f(10) =$ highest prime factor of $10 = 5$</p> <p>$f(11) =$ highest prime factor of $11 = 11$</p> <p>$f(12) =$ highest prime factor of $12 = 3$</p> <p>$f(13) =$ highest prime factor of $13 = 13$</p> <p>\therefore Range $= \{3,5,11,13\}$ ans.</p>	
Q.19)	Let f be a subset of $z \times z$ defined by $f = \{(ab, a + b): a, b \in z\}$. Is f a function? Justify your answer.	
Sol.19)	<p>We have, $f = \{(ab, a + b): a, b \in z\}$</p> <p>Let $a = 2$ & $b = 3$</p> <p>$\therefore ab = 6$ and $(a + b) = 5$</p> <p>$\therefore (6,5) \in f$</p> <p>Now, let $a = 6$ and $(a + b) = 7$</p> <p>$\therefore (6,7) \in f$</p> <p>$\Rightarrow (6,5) \in f$ and $(6,7) \in f$</p> <p>It means element 6 has two different images 5 and 7</p> <p>$\therefore f$ is not a function ans.</p>	